

# A Parsimonious Model of Mobile Partitioned Networks with Clustering

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# Models and Algorithms for Mobile Networks





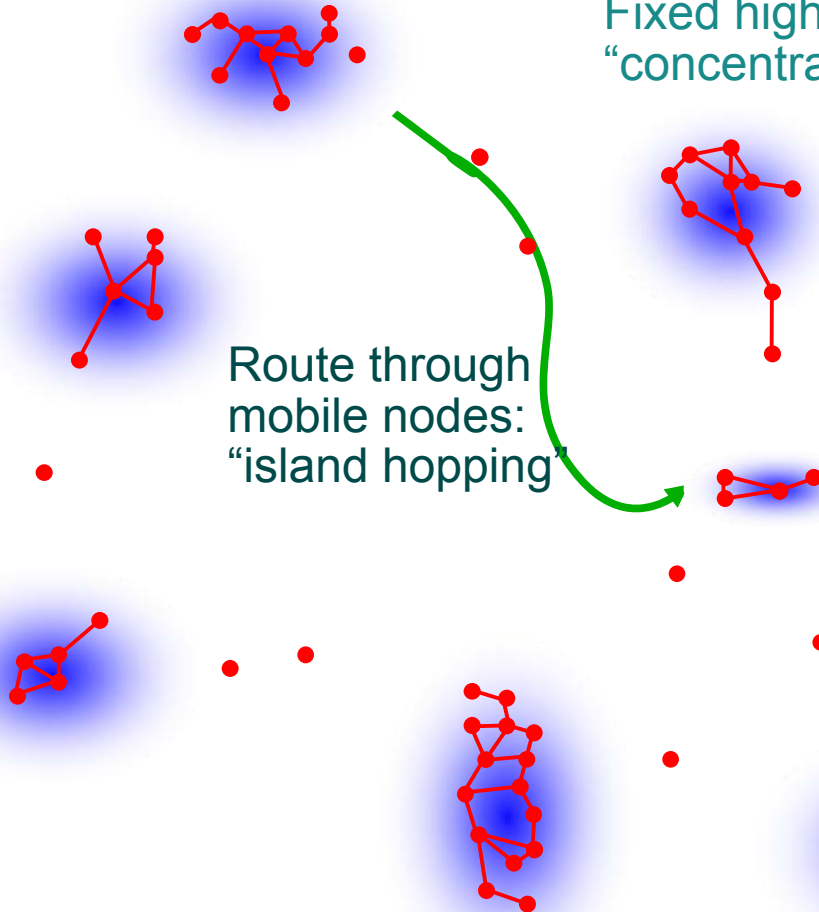
# Models and Algorithms for Mobile Networks

- **Mobile Wireless Networks are different:**
  - No wires -> no links
  - Mobility -> uncertainty
  - Heterogeneity -> partition
- **Contribution**
  - A simple & tractable model capturing heterogeneity in connectivity and in mobility
  - Validation through data
  - Insights into DTN routing design space

# Routing in Partitioned Networks



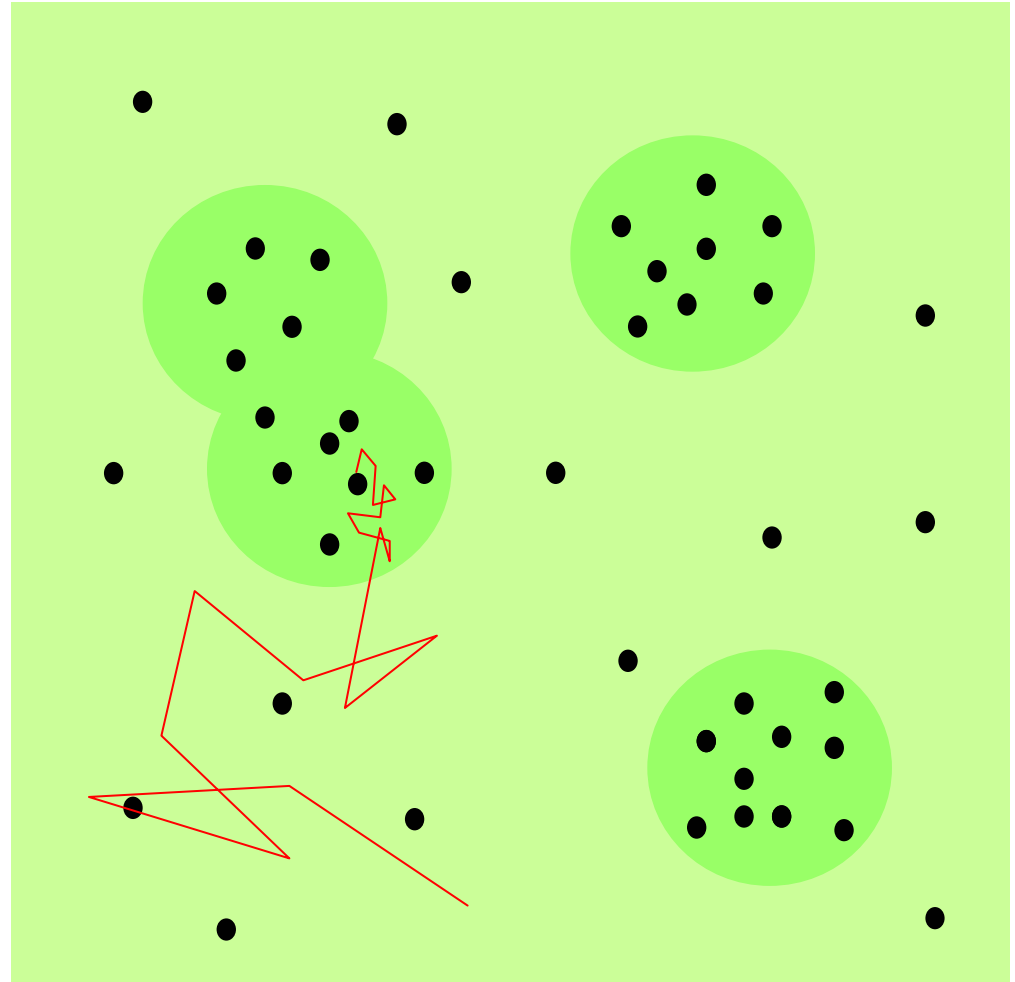
Fixed high-density island =  
“concentration points”



- Goal:
  - Designing robust DTN routing algorithms

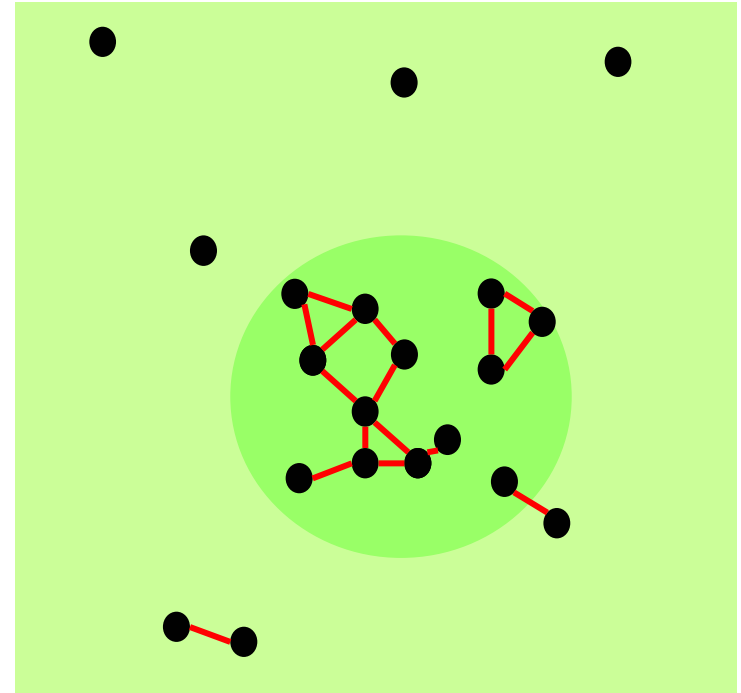
# Heterogeneous Random Walk Model

- **Definition:**
  - $n$  nodes on square torus
  - Each node performs independent (scaled) Brownian motion
  - Fixed regions  $A_l$  where mobility is slower, and  $A_h$  where it is faster
  - For example,  $A_l = m$  random disks



# HRW Model: Main Properties

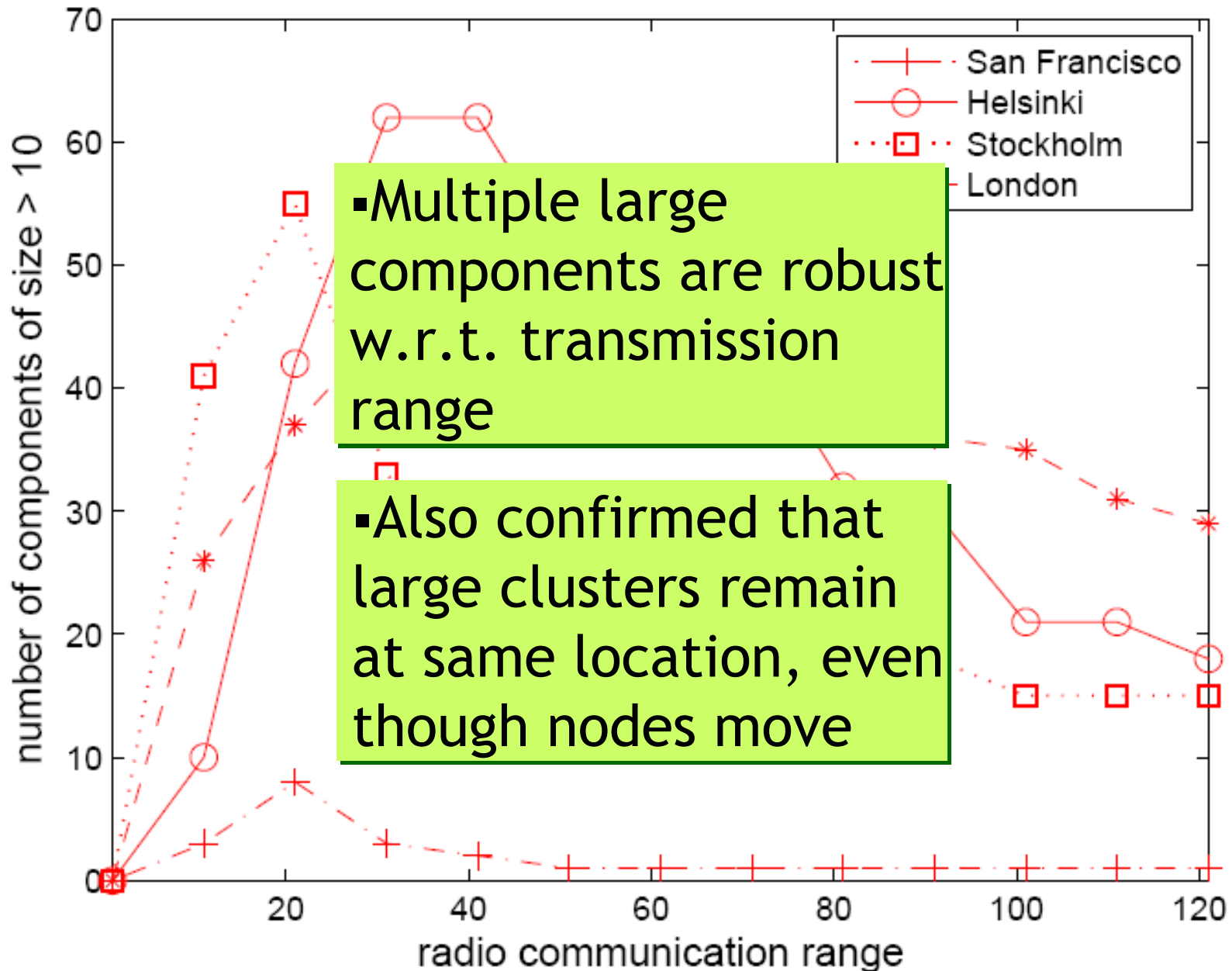
- **Stationary distribution**
  - $\Pi_{l,h} \sim \sigma_{l,h}^{-2}$
  - Density inverse of speed
- **Connectivity**
  - Rich connectivity inside  $A_l$ , scarce connectivity outside
  - Continuous percolation: ensure supercritical density in  $A_l$ , subcritical in  $A_h$
  - $\lambda_{l,h} r^2 = n \sigma_{l,h}^{-2} r^2 \ll (\lambda r^2)_{cr} \approx 1.43$
- **Discrete-time version and “perfect simulation”**
  - Correction when crossing boundary
  - Starting simulation without transient



# Validation

- **Data set:**
  - Fine-grained mobility of taxi cabs in the San Francisco Bay Area
  - 500 cars over one month
  - Position updates approx. every 10 sec
  - Other traces from Nokia Sportstracker dataset
- **Verifying features of model:**
  - Robustness and stability of clusters (persistent components)
  - Similarity of node mobility patterns
  - Speed-density relationship

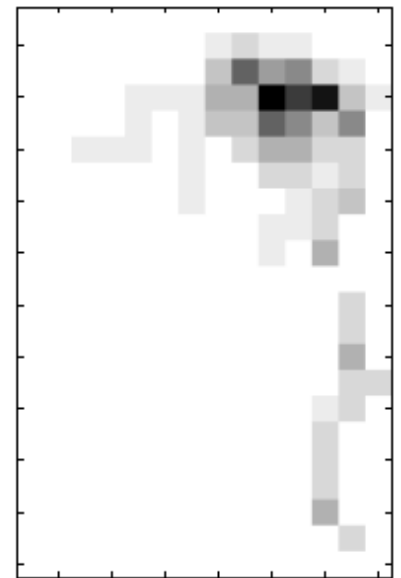
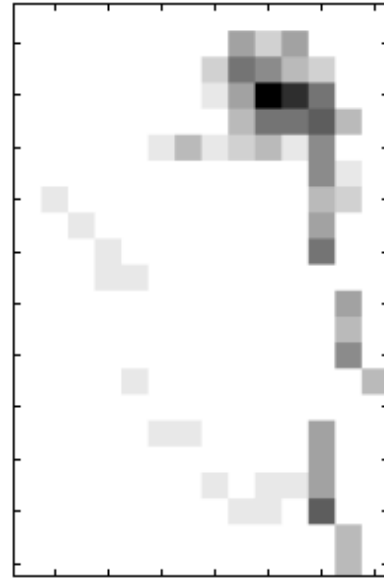
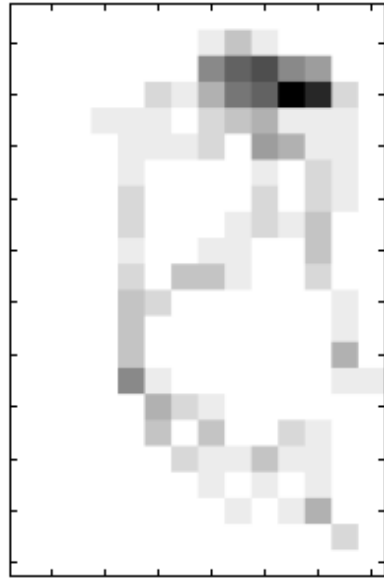
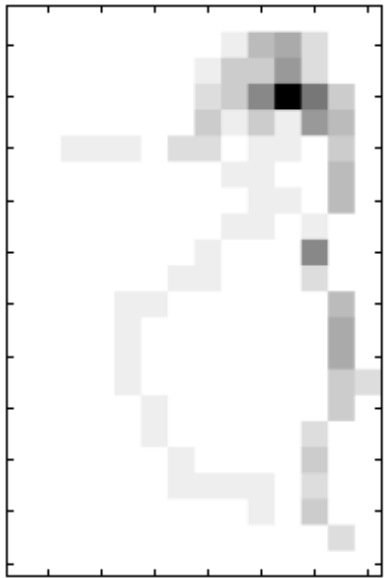
# Number of Components vs Radio Range



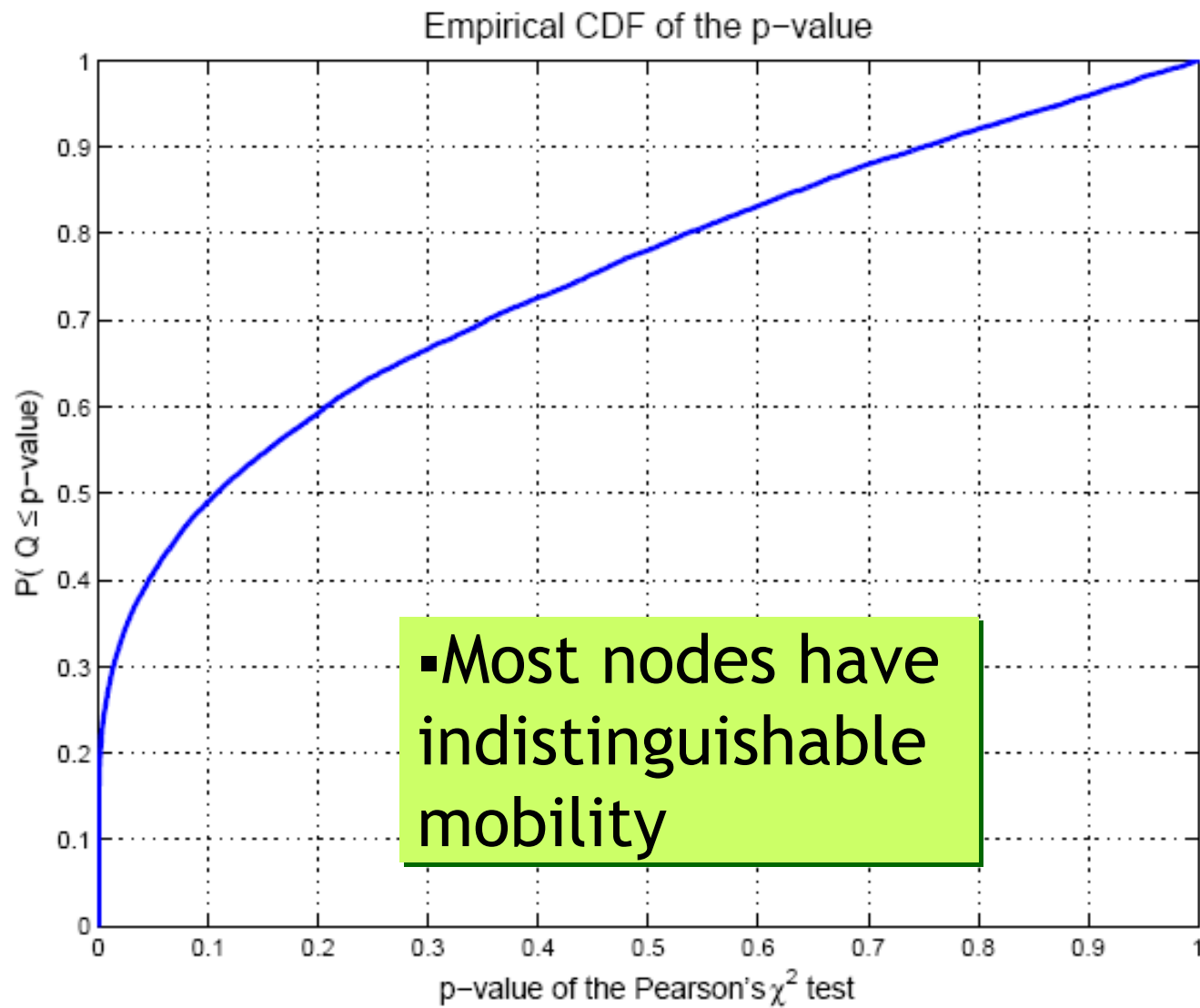


# Statistical Similarity of Node Mobility

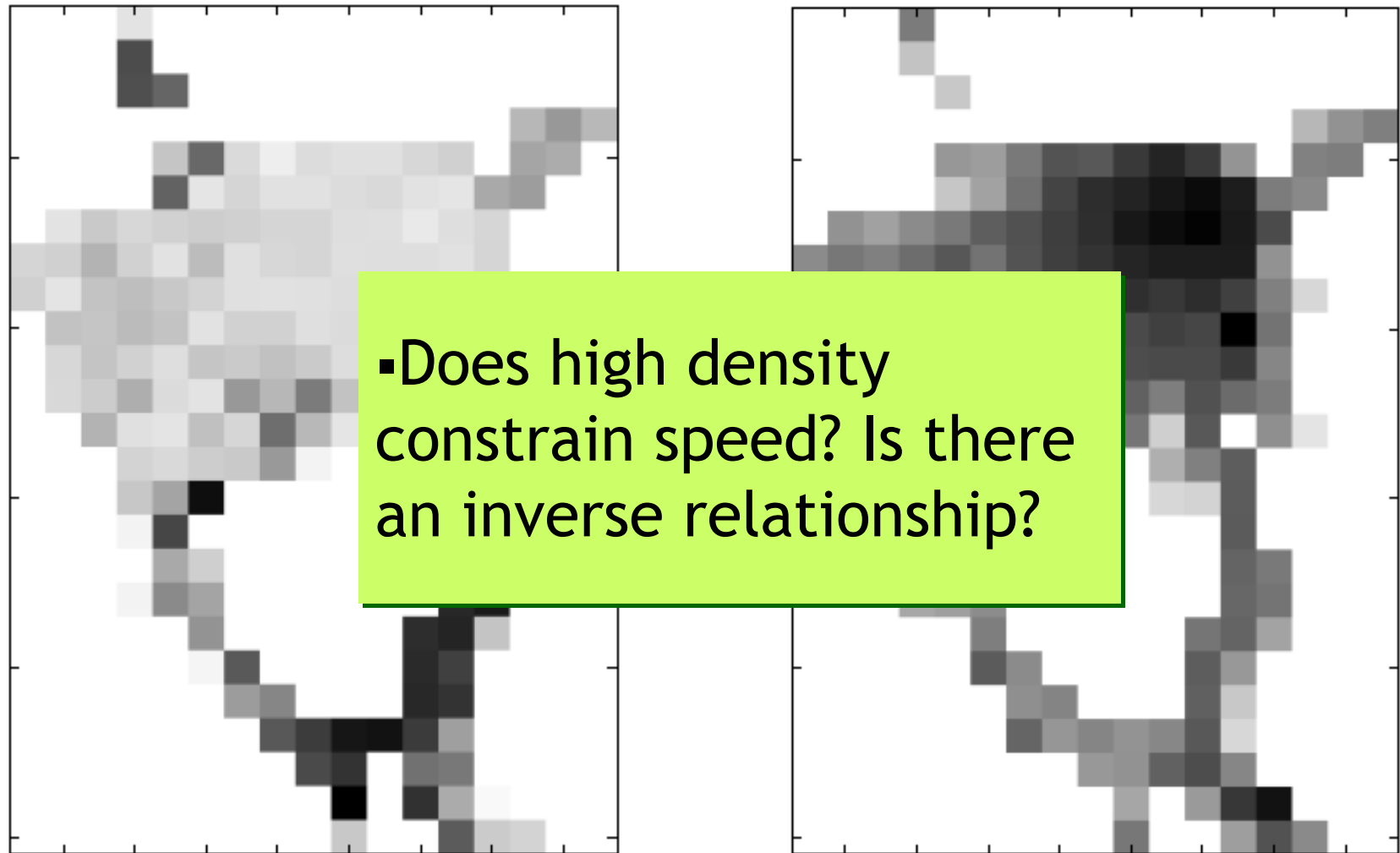
- One-day snapshots of individual visits to cells



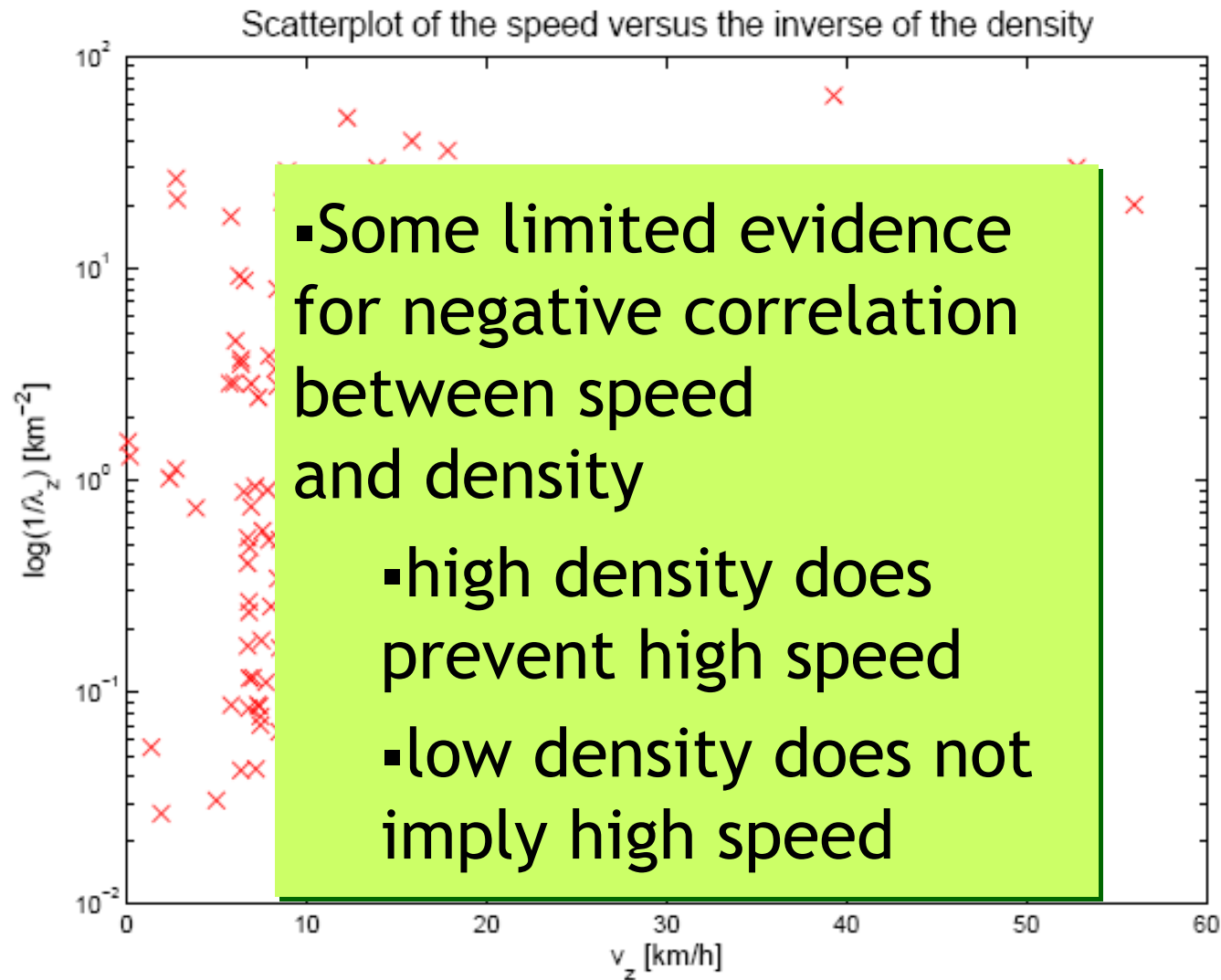
# $\chi^2$ -Test: Similarity of Marginal Distributions



# Speed and Density Maps

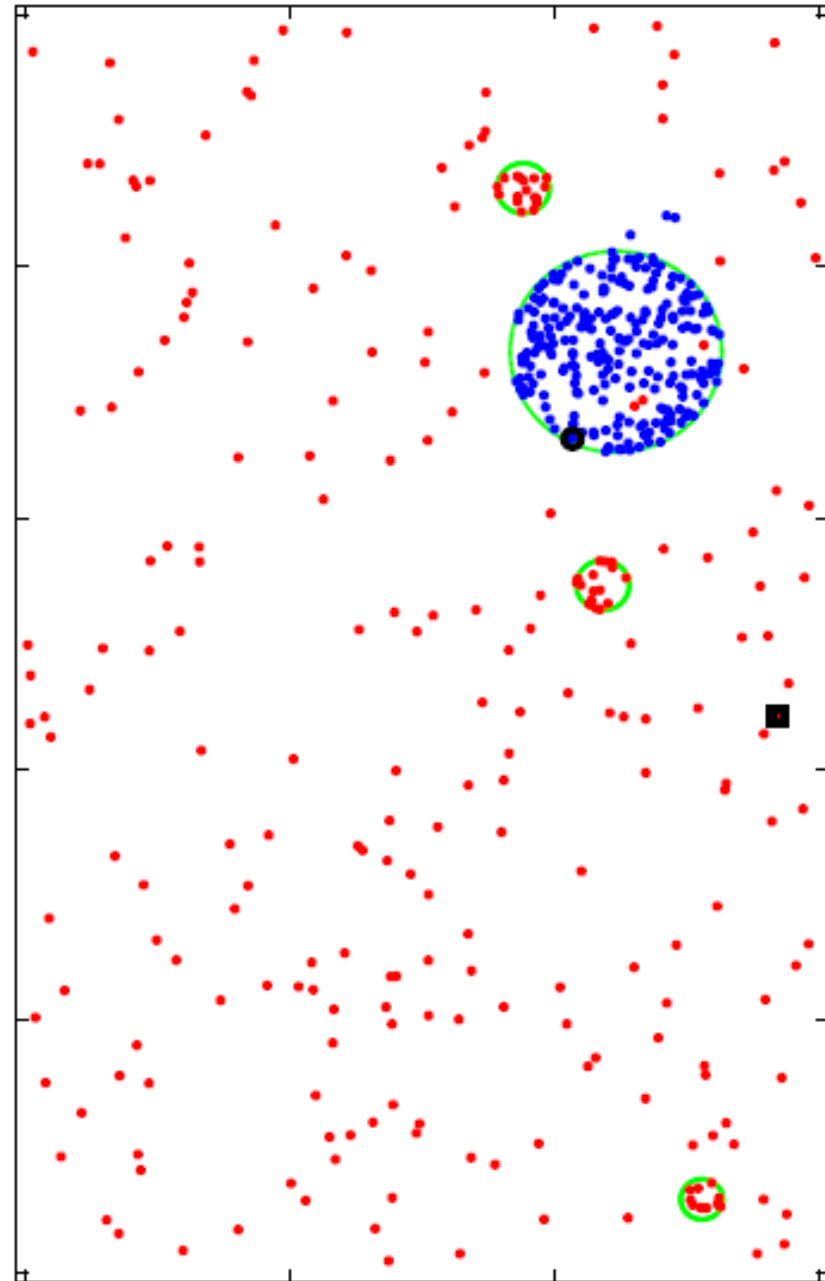


# Speed and Density Scatter Plot



# Example: Epidemic Dissemination

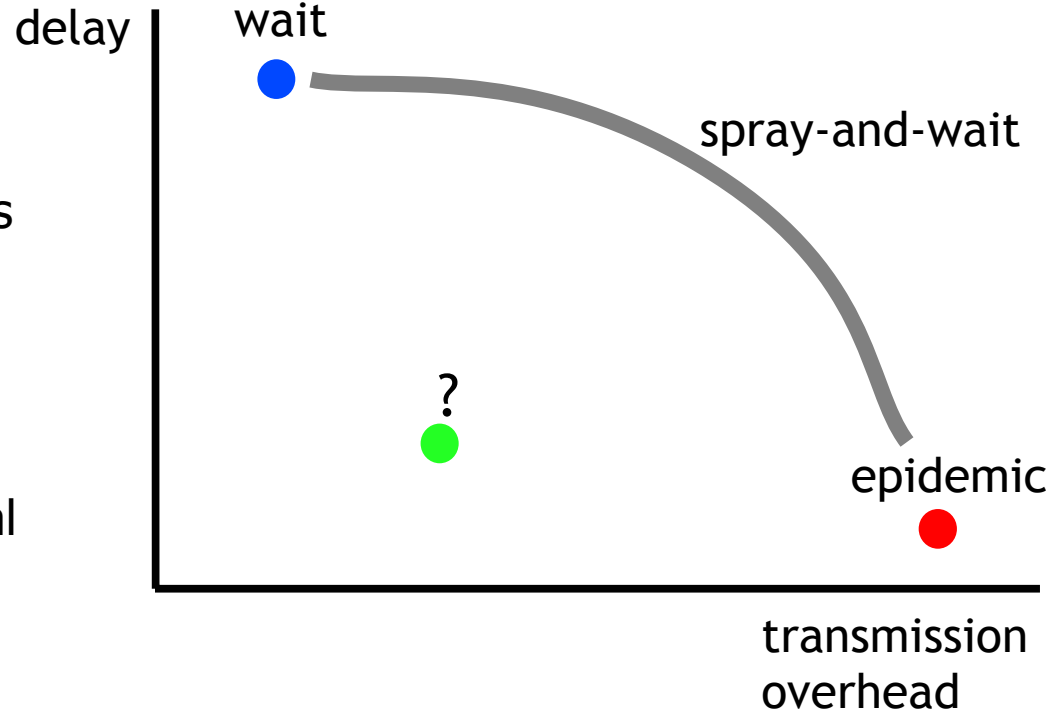
- **Experiment: fit model to trace**
  - $A_l$  = highly connected areas
  - match average speed separately in  $A_l$  and  $A_h$
- **Metrics:**
  - delay, overhead (# copies), min-delay-path length
- **Comparison:**
  - Random walk
  - Random waypoint
- **Result:**
  - HRW best overall predictor





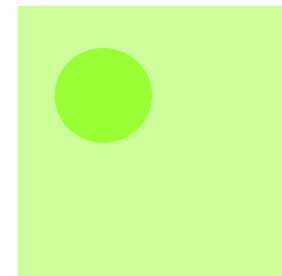
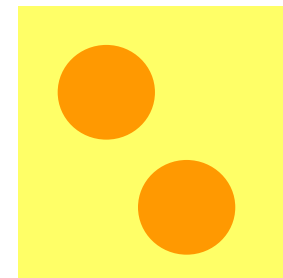
# DTN Routing under Random Walk Mobility

- Design space of DTN routing algorithms:
  - Single or multiple copy
  - Forward and/or copy decisions
  - Control information (e.g., encounter frequency)
- HRW: Markov chain, state = location
  - No “predictability” of individual node’s future movements
  - Given current location, every node is equivalent
- Question:
  - Can we actually route in such a model, i.e., do better than random dissemination?
  - If we can, what information should nodes collect and exchange?

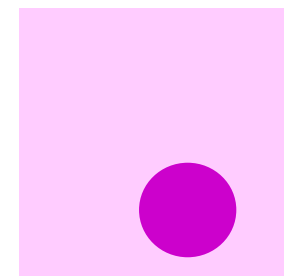


# Single Copy and Spray-and-Wait in HRW Mobility

- **HRW model:**
  - Single copy: no benefit in relaying copy -> no control information needed
  - Spray-and-wait: set of relays is irrelevant -> min of i.i.d. delays
- **Beating spray-and-wait boundary**
  - Requires “continuous multi-copy” scheme, i.e., decisions after realization
- **Contrast with node-heterogeneous model:**
  - Assume each node has its own preferred (set of) location(s)
  - All indep. random walks, same aggregate node density
  - But: single copy and spray-and-wait benefits from control information

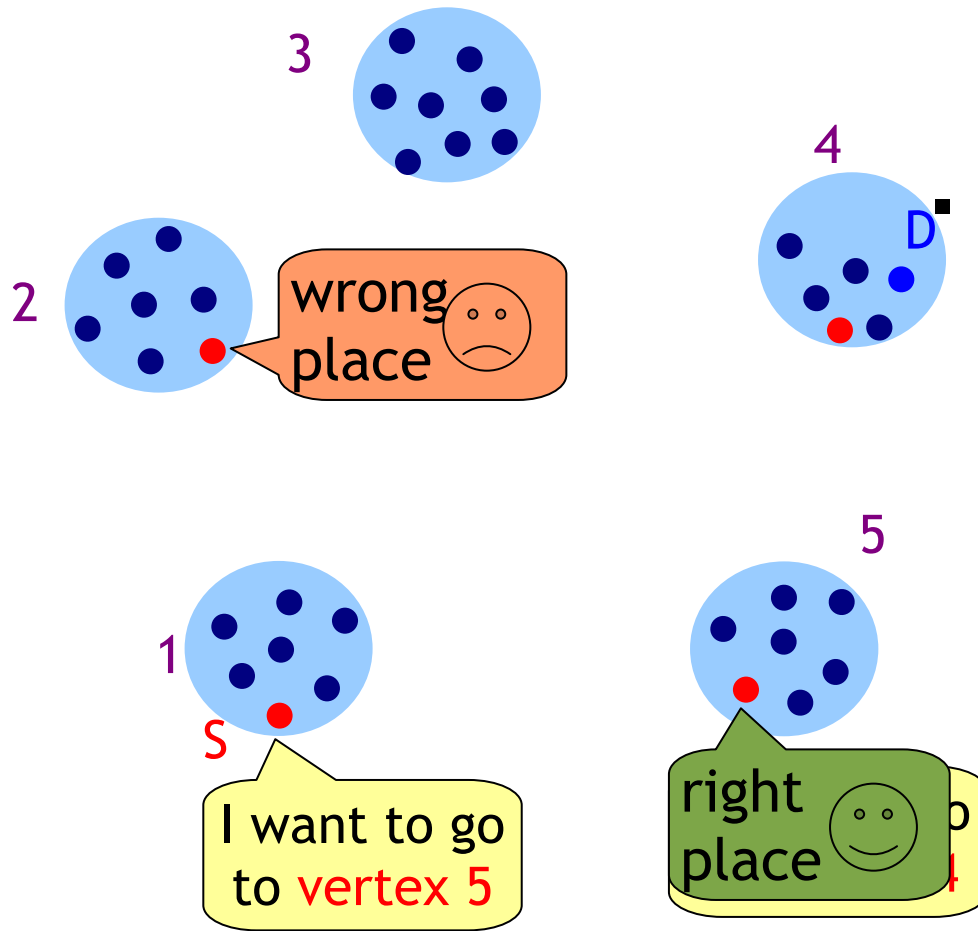


class 1



class 2

# Beating Spray-and-Wait with HRW Mobility



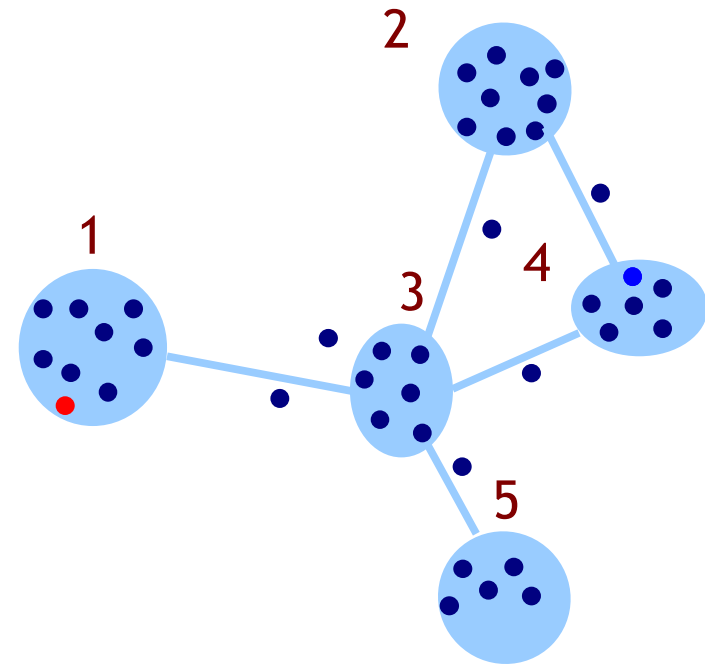
## Problem:

- How to make predictable progress under unpredictable mobility?

## Key idea:

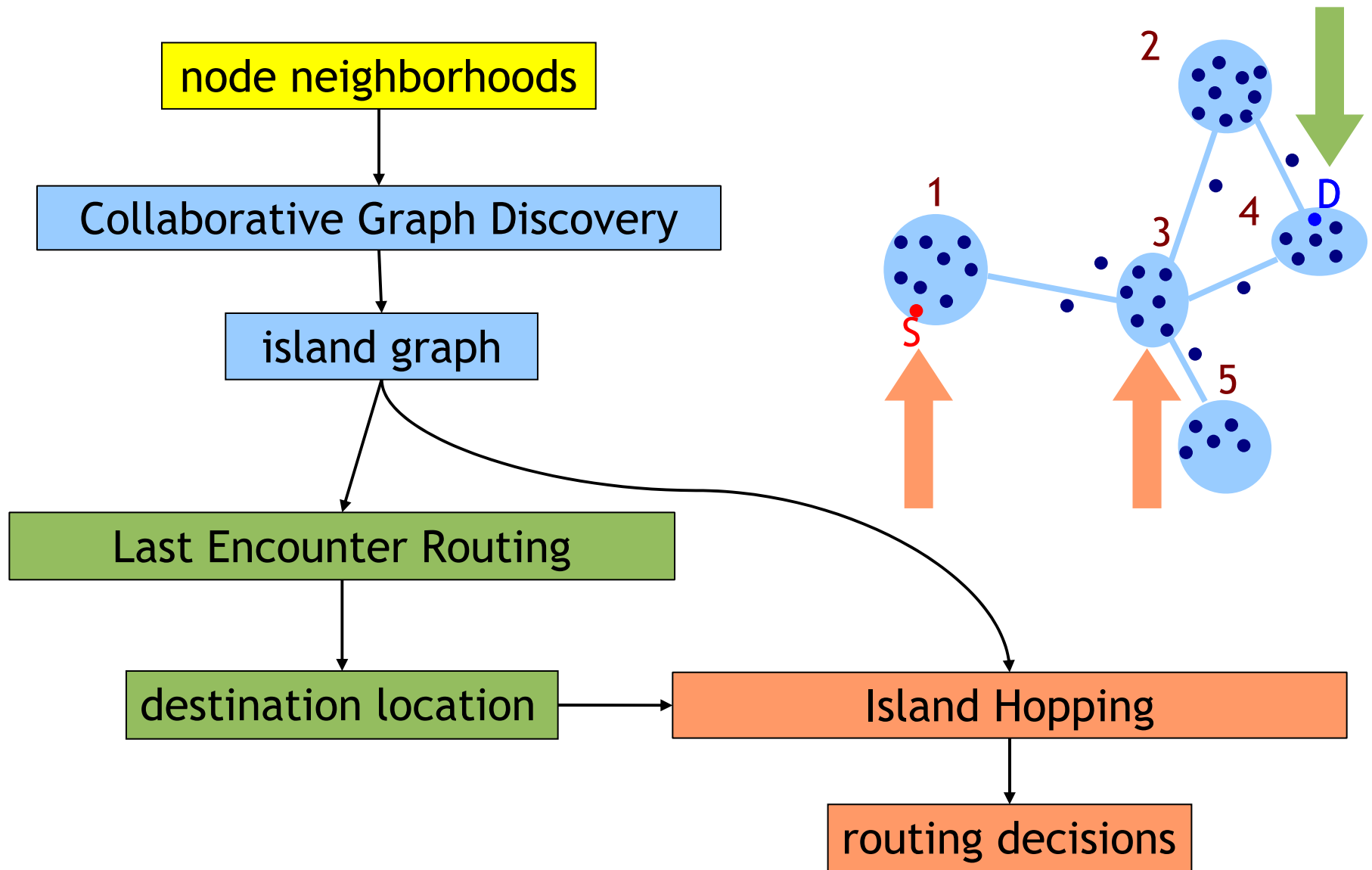
- Cannot control mobility of individual message
- But can control mobility of set of copies of a message
- Deferred copy and kill decisions at islands

# Collaborative Graph Discovery



- Assume no external signal
  - No GPS or fixed beacon
  - No information about movement of self and others
- Collaborative graph discovery:
  - Stable islands with high connectivity: natural “beacons”!
  - Derive island graph only from observation of neighbors
- Key idea:
  - Vertex labeling:
    - Assign unique labels to islands
    - Maintain the labels stable as long as possible -> “voting for labels”
  - Edge Discovery:
    - Discover the labeled edges of the CP graph
    - Gossiping, aging, handling error conditions

# Island Hopping for DTN Routing





# Key Points

- **Real DTN scenarios are heterogeneous**
  - Node mobility, connectivity
- **HRW model:**
  - Corner case: homogeneous nodes, heterogeneous space
  - Stable islands of connectivity, but “maximally unpredictable” nodes
  - Parsimonious, tractable
- **Validation**
  - San Francisco taxi trace + Nokia Sportstracker traces
  - Statistical similarity of nodes, clustering vs range, speed-density
  - Capturing “high connectivity” and “high mobility” regions
- **Routing:**
  - Random Walk: no predictability for individual nodes
  - But “deferred multi-copy” schemes can perform well
  - Optimal scheme and control information are open questions

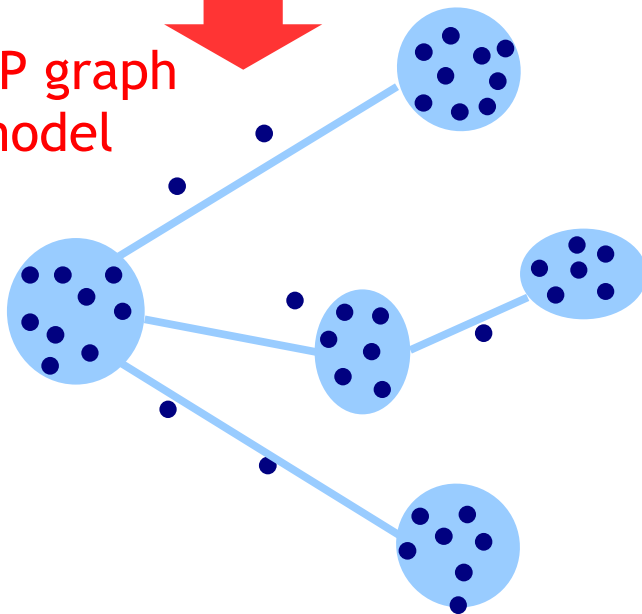
# Backup

# Stable Concentration Points

## Mobility traces



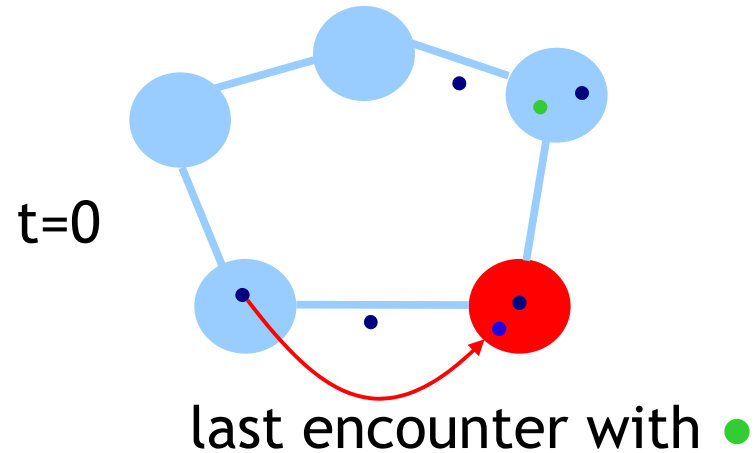
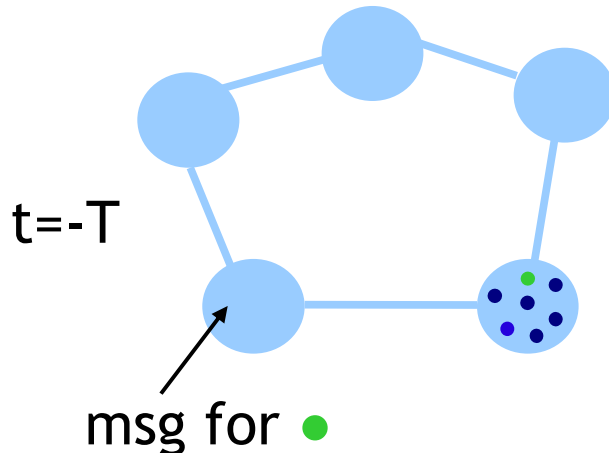
## CP graph model



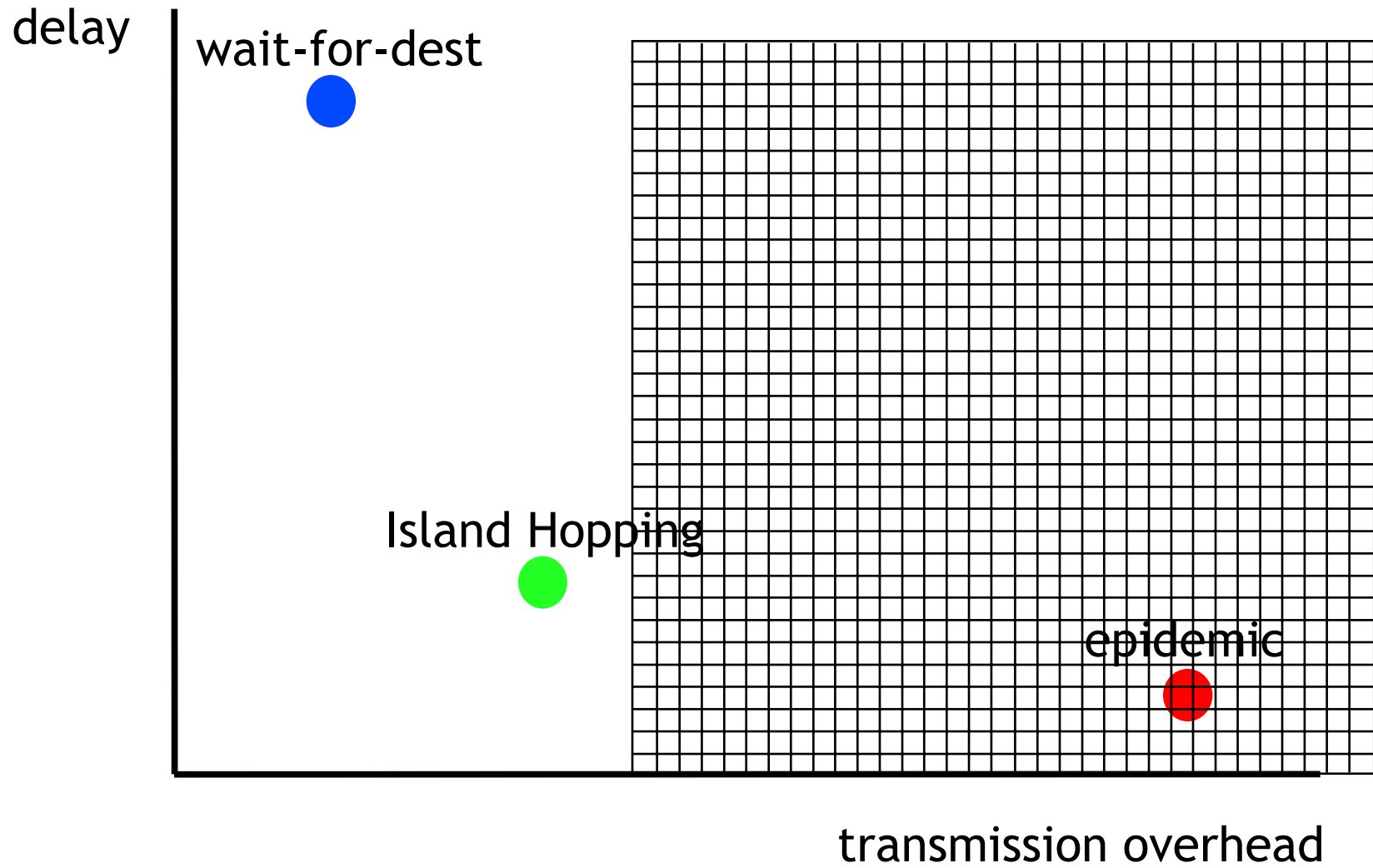
- **CP graph:**
  - Vertices = CPs
  - Edges = flows of nodes between CPs
- **Worst-case connectivity & mobility model:**
  - Only nodes at the same vertex can communicate
  - A node in transit can not communicate with anyone
  - Nodes perform independent random walks on CP graph

# Island Hopping through Mobility

- Only way from island to island is through movement of nodes
  - But how? Obvious approaches:
    - Epidemic: Flood entire network -> fast but costly
    - Wait-for-dest: slow but cheap
  - Make smart "hitchhiking decisions"
    - How to find the destination in a disconnected network?
    - Last Encounter routing on the CP graph
      - > try to move in "the right direction"



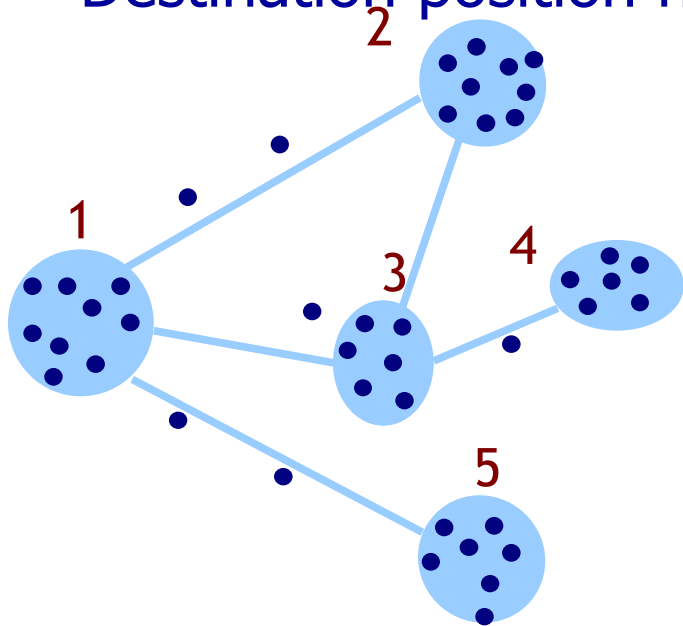
# Island-Hopping: Delay-Overhead Sweetspot





# Execution Example COGRAD + IH

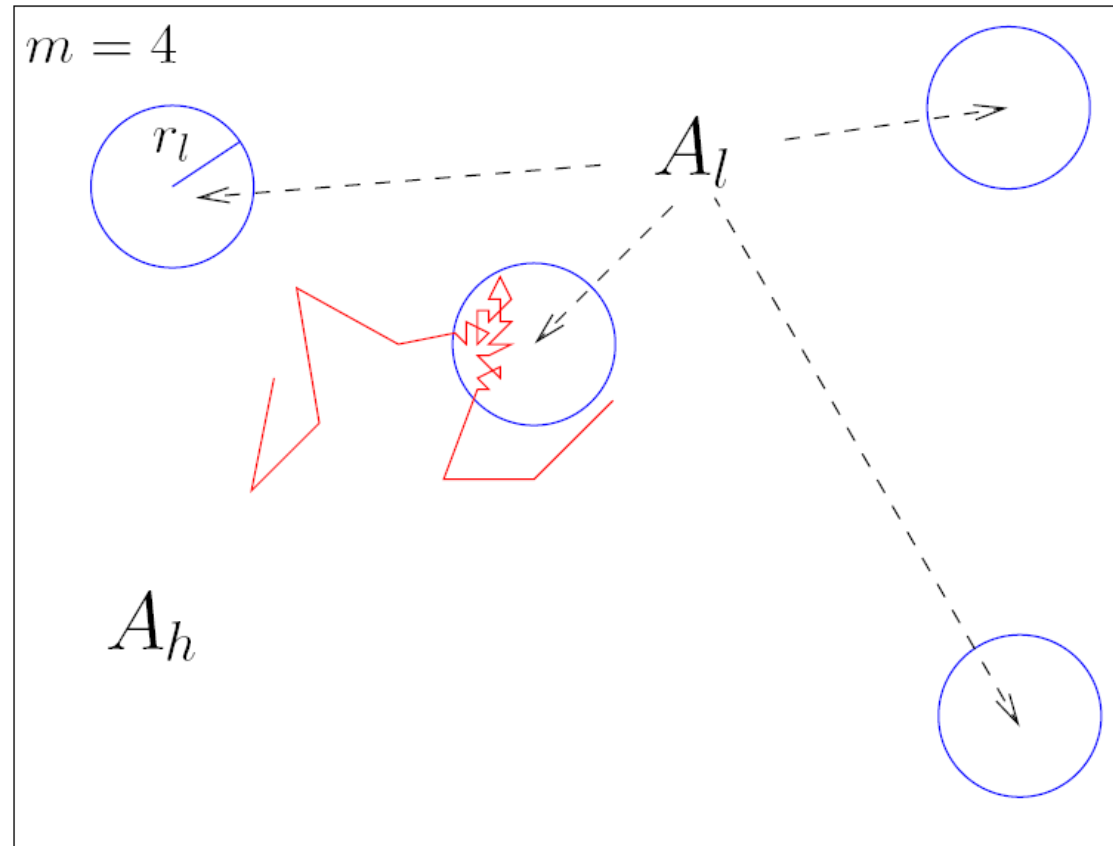
- 500 nodes on a 5x5 grid of concentration points
- No positioning information available to nodes
- Grid topology not known to nodes
- Destination position not known to nodes



# Summary: Partitioned Mobile Networks

## References:

- Last Encounter Routing  
EASE: Learning Efficient  
IEEE/ACM Trans. on Ne
- [Sarafijanovic-Djukic, Pi  
Mobility-Assisted Forward  
2006]



# Conclusion

- **Models for main aspects of mobile wireless networks**
  - Model 1: Optimal Opportunistic Routing
  - Model 2: Routing under Mobility
  - Model 3: Partitions
- **The right abstraction is half the solution**
  - Depends on the problem
  - Should inform the solution
- **Future research:**
  - Heterogeneity and asymmetry: energy, communication, computation
  - Hybrid scenarios
  - Addressing information vs network entities: overlays, pub-sub,...